

Egyptian multiplication

Multiplication by doubling, halving and some bookkeeping.
Recursive and iterative versions

1 Recursive version

```
(%i1) Egyptian_multiplication(a, b) :=
  (if verbose then printf(true, "~10d ~10d ~%", a, b),
  if a=1
  then b
  else (if mod(a, 2) = 0
        then Egyptian_multiplication(a/2, 2*b)
        else b + Egyptian_multiplication(a-1, b) ) ) $ ;
```

```
(%i2) verbose : true /* global control variable */ $
```

```
(%i3) Egyptian_multiplication(60,4);
```

```
 60    4
 30    8
 15   16
 14   16
 7   32
 6   32
 3   64
 2   64
 1  128
```

```
(%o3) 240
```

```
(%i4) verbose : false $
```

```
(%i5) Egyptian_multiplication(80,4);
```

```
(%o5) 320
```

```
(%i6) (verbose : true, Egyptian_multiplication(92, 15) ) ;
```

```
 92    15
 46    30
 23    60
 22    60
 11   120
 10   120
 5   240
 4   240
 2   480
 1   960
```

```
(%o6) 1380
```

```
(%i7) (verbose : false, Egyptian_multiplication(92, 15) );
```

```
(%o7) 1380
```

2 Iterative version

```
(%i8) Egyptian_multiplication_iterative(a,b) :=
```

```
  block([a1 : a, b1 : b, c : 0 ],
```

```
  while a1 > 1 do
```

```
    (if verbose then printf(true, "~10d ~10d ~10d ~%", a1, b1, c),
```

```
    if mod(a1, 2)=0
```

```
      then (a1 : a1/2, b1 : b1*2)
```

```
      else (a1 : a1-1, c : c+b1) ),
```

```
    if verbose then printf(true, "~10d ~10d ~10d ~%", a1, b1, c),
```

```
    b1+c ) $ ;
```

```
(%i9) (verbose : true, Egyptian_multiplication_iterative(92,15)) ;
```

```

92    15    0
46    30    0
23    60    0
22    60    60
11   120    60
10   120   180
5    240   180
4    240   420
2    480   420
1    960   420
```

```
(%o9) 1380
```

```
(%i10) (verbose : false, Egyptian_multiplication_iterative(92,5)) ;
```

```
(%o10) 460
```